VGP351 – Week 2

Agenda:

- Getting data to the GPU
- Types of primitives
- Transformations
 - Modeling
 - Viewing
 - Projection



Graphics Pipeline



Graphics Pipeline



Memory Architecture



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Memory Architecture



Unified Memory Architecture



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Memory Map



Memory Map



Vertex Memory

Practically, the GPU can only access:

- Memory physically on the graphics card
- Memory mapped in the GART
- To get GART or card memory, we have to allocate it using the driver
 - Only the driver knows what kind of memory to use
 - ...but we have to give it some hints



Vertex Memory

In OpenGL this memory is called *buffer object*

- It is used somewhat like a file:
 - Bulk I/O via accessor routines
 - Direct mapping and access via a pointer



Generate "names" for the buffer objects:
 glGenBuffers(GLsizei num, Gluint *names);

"Bind" a buffer for use:

glBindBuffer(GLenum target, GLuint name);

target selects which buffer we're talking about

- GL_ARRAY_BUFFER is used for vertex data
- GL_ELEMENT_ARRAY_BUFFER is used for vertex indices

More on that *later*...

- There are other targets we'll cover later in the term
- Binding creates the object, but it still has no storage

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Storage is created and optionally initialized with: void glBufferData(GLenum target, GLsizeiptr size, const GLvoid *data, GLenum usage); - usage tells the GL how the app will utilize the buffer Storage is updated with: void glBufferSubData(GLenum target, GLintptr offset, GLsizeiptr size, const GLvoid *data);

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Usage conveys information along two axes:

- Data "frequency":
 - Stream data is specified once and used a few times
 - Static data is specified ones and used many times
 - Dynamic data is specified and used many times
- Data "usage":
 - Draw data used as source for drawing
 - Read data copied from GL and read back to client
 - Copy data copied from GL and used as source for drawing
- Combine these to create the enums (e.g., GL_STATIC_DRAW)

Memory backing the buffer can be mapped into CPU space:

GLvoid *glMapBuffer(GLenum target,

GLenum access);

- access tells the driver how the application will access the mapped buffer:
 - GL_READ_ONLY
 - GL_WRITE_ONLY
 - GL_READ_WRITE
- Unmap the buffer with:

GLboolean glUnmapBuffer(GLenum target);

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Now what?

The vertex data is in a buffer object...how do we tell the GPU know where to get it?

Set the location and format of a vertex attribute with:

void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

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void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer); In the API, attributes are

numbered

Set the location and format of a vertex attribute with:

void glVertexAttribPointer(GLuint index,

GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

Number of components in each element

Type of data (e.g., GL_FLOAT)

Set the location and format of a vertex attribute with:

void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

> For integer data, specifies whether it is normalized or not

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Set the location and format of a vertex attribute with:

void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

> Number of bytes from the start of one element to the start of the next

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Set the location and format of a vertex attribute with:

void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

Offset, in bytes, from the start of the buffer where the data starts

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Enable Attribute

Attributes that will be used must also be enabled:

void glEnableVertexAttribArray(GLuint index);

Attributes can later be disabled: void glDisableVertexAttribArray(GLuint index);



Setting Attribute Numbers

GLSL uses names for attributes:

attribute vec4 color;

The API uses numbers:

void glVertexAttribPointer(GLuint index, GLint size, GLenum type, GLboolean normalized, GLsizei stride, const GLvoid *pointer);

How do we connect the two?

Setting Attribute Numbers

Bind the attribute name to the index we want: void glBindAttribLocation(GLuint programObj, GLuint index, const GLchar *name);

- Can only call *after* linking the program
- See also program::bind_attrib_location



Drawing

Draw a series of vertices: void glDrawArrays(GLenum mode, GLint first, GLsizei count);



Drawing

Draw a series of vertices: void glDrawArrays(GLenum mode, GLint first, GLsizei count); Sets the primitive type

Drawing

Draw a series of vertices: void glDrawArrays(GLenum mode, GLint first, GLsizei count); Number of Selects which vertex vertices to draw in the buffer to start drawing with

Primitive Types



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Primitive Types



Image borrowed from "OpenGL Programming Guide". 22-January-2009 © Copyright Ian D. Romanick 2009

References

More information about I/O MMUs in general: http://en.wikipedia.org/wiki/IOMMU

Nvidia whitepaper about using VBOs: http://developer.nvidia.com/object/using_VBOs.html



Break

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Linear Algebra Primer

Three important data types:

- Scalar values
- Row / column vectors
 - 1x4 and 4x1 are the most common sizes
- Square matrices
 - 4x4 is the most common size...to match the 1x4 & 4x1 vectors



Row Vectors

These are special matrices that have multiple columns but only one row

– Example: [5.0 3.14 37]

Addition and subtraction is component-wise:
Example: [1 2 3]+[9 10 11]=[10 12 14]

- Both vectors must be the same size
- Operations with scalars also component-wise:
 - Example: $3.2 \times \begin{bmatrix} 1 & 2 & 3 \end{bmatrix} = \begin{bmatrix} 3.2 & 6.4 & 9.6 \end{bmatrix}$

Notice that vector multiplication is missing...

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Column Vectors

These are special matrices that have multiple rows but only one column

- Example: 1 2 3
- Work just like row vectors
- Notationally convert a row to a column with a T in the exponent
 - Example: V^{T}

Vector Operations

- There are a few operations specific to vectors that are really important to graphics:
 - Dot product
 - Vector magnitude / normalization
 - Cross product



Dot Product

Noted as a "dot" between two vectors (e.g., A•B)

- Also known as the inner product
- Component-wise multiply, then sum components
 - Example:

 $\begin{bmatrix} 2.3 & 1.2 \end{bmatrix} \cdot \begin{bmatrix} 1.7 & 6.5 \end{bmatrix} = (2.3 * 1.7) + (1.2 * 6.5) = 11.71$


Vector Magnitude

Noted by vertical bars around the vector

- Like absolute value...which is the scalar magnitude
- Can also be thought of as the length of the vector
- Square-root of dot-product of vector with itself
 - Like absolute value

Example:
$$\left\| \frac{\sqrt{2}}{2} \quad \frac{\sqrt{2}}{2} \right\| = \sqrt{\left[\frac{\sqrt{2}}{2} \quad \frac{\sqrt{2}}{2} \right]} \cdot \left[\frac{\sqrt{2}}{2} \quad \frac{\sqrt{2}}{2} \right] = \sqrt{\left(\frac{\sqrt{2}}{2} \right)^2} + \left(\frac{\sqrt{2}}{2} \right)^2 + \left(\frac{\sqrt{2}}{2} \right)^2 = \sqrt{\frac{2}{4}} + \frac{2}{4} = 1$$

Normal

- Normal is an overloaded term in graphics and linear algebra
 - Sometimes it means a vector has unit length
 - |A| = 1.0
 - Can say the vector is "normalized"
 - Sometimes it means a vector is perpendicular to a surface or another vector
 - This mean the angle between the vectors is 90°
 - Can say that the vectors are "normal to each other"
 - Can say that the vectors are "orthogonal"
 - Can combine for even more fun!

Use normalized surface normals in the calculation." ^{22-January-2009}

Normalize

- Can normalize a vector by dividing it by its magnitude
 - Example: $\frac{A}{|A|}$
 - Vector has the same direction, but the magnitude will be 1.0
 - Also works with scalars



Dot Product

Why is the dot product so interesting?

Dot Product

Why is the dot product so interesting?

- The dot product of two vectors is related to the cosine of the angle between those vectors
- Formally: $A \cdot B = |A| |B| \cos \theta$
- We often want to know the angle between two vectors
 - This is the basis of all lighting calculations in 3D graphics!
 - $(A \bullet B) / (|A| |B|) = \cos \theta$

Cross Product

From Wikipedia:

In mathematics, the cross product is a binary operation on two vectors in a three-dimensional Euclidean space that results in another vector which is perpendicular to the plane containing the two input vectors.

- Noted as an \times between two vectors
- Calculated as:

$$a \times b = \begin{bmatrix} a_y b_z - a_z b_y & a_z b_x - a_x b_z & a_x b_y - a_y b_x \end{bmatrix}$$

- Not associative
- Anti-commutative: If $A \times B = C$, then $B \times A = -C$

¹ From http://en.wikipedia.org/wiki/Cross_product 22-January-2009 © Copyright I<u>an D. Romanick 2009</u>

Cross Product

Why is the cross product so interesting?

- Cross product of two vectors results in a new vector that is normal both
- The cross product of two vectors is related to the sine of the angle between the vectors

A

- Formally: $A \times B = |A| |B| \sin \theta$ n



Matrices

Like vectors, but have multiple rows and columns

- Add and subtract like you would expect
 - Like vectors, both matrices must be the same size...in both dimensions

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Matrix Multiplication

- Special rules make matrix multiplication different from scalar multiplication
 - **NOT** commutative! e.g., $M \times N \neq N \times M$
 - Associative e.g., A(BC) = (AB)C
 - Column count of first matrix must match row count of second matrix
 - If *M* is 4-by-3 matrix and *N* is a 3-by-1 matrix, we can do $M \times N$ but not $N \times M$
 - If the source matrices are n-by-m and m-by-p, the resulting matrix will be n-by-p

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Matrix Multiplication

To calculate an element of the matrix, C, resulting from AB:

$$C_{ij} = \sum_{r=1}^{n} a_{ir} b_{rj}$$

What does this look like?



Matrix Multiplication

To calculate an element of the matrix, C, resulting from AB:

$$C_{ij} = \sum_{r=1}^{n} a_{ir} b_{rj}$$

What does this look like?

- The dot product of a row of A with a column of B!
- This is why the column count of A must match the row count of B...otherwise the dot product wouldn't work



Multiplicative Identity

There is a multiplicative identity for matrices

$$I = \begin{bmatrix} 1 & 0 & \cdots & 0 \\ 0 & 1 & & \vdots \\ \vdots & & \ddots & 0 \\ 0 & 0 & \cdots & 1 \end{bmatrix}$$

- Just like any other multiplicative identity, AI = A
- If you pretend that a scalar is a 1×1 matrix, this should make sense

Transpose

- Rows become columns and columns become rows
 - Noted with a T in the exponent position (e.g., M^{T})
 - Example:

$$\begin{bmatrix} 2 & 3 \\ 4 & 5 \\ 6 & 7 \end{bmatrix}^{T} = \begin{bmatrix} 2 & 4 & 6 \\ 3 & 5 & 7 \end{bmatrix}$$

References

http://en.wikipedia.org/wiki/Matrix_multiplication http://en.wikipedia.org/wiki/Dot_product http://en.wikipedia.org/wiki/Cross_product



Rotation around the Z-ax	(is
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- If θ is 0, this is the identity matrix

 $\begin{bmatrix} \cos\theta & -\sin\theta & 0 & 0\\ \sin\theta & \cos\theta & 0 & 0\\ 0 & 0 & 1 & 0\\ 0 & 0 & 0 & 1 \end{bmatrix}$

Rotation around the Y-axis

- From the previous equations, we can rotate using 4 multiplies and 2 adds, but a matrix multiply requires 16 multiplies and 12 adds
 - $x' = x \cos \theta + y \sin \theta$
 - $-x' = -x \sin \theta + y \cos \theta$
 - -z'=z
- Why use the matrix method?



A series of rotations can be implemented as:

 $v' = M_1 v$ $v'' = M_2 v'$ $v''' = M_3 v''$

- Vhich is the same as: $M_3(M_2(M_1v))$
- What can we do with this?

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A series of rotations can be implemented as:

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- Vhat can we do with this? $(M_3M_2M_1)v$
 - Matrix multiplication is associative!

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Arbitrary Rotation

Siven a vector, v, and an angle, θ , we can create an arbitrary rotation matrix:

$$\tilde{v} = \begin{bmatrix} 0 & -v_{z} & v_{y} & 0 \\ v_{z} & 0 & -v_{x} & 0 \\ -v_{y} & v_{x} & 0 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$
$$R = (I * \cos \theta) - ((1 - \cos \theta) * (v * v^{T})) + (\sin \theta * \tilde{v})$$

Translation

- Points are stored as p = [x y z 1]
- Remember the definition of matrix multiplication:

$$p_{x}' = p_{x} M_{11} + p_{y} M_{12} + p_{z} M_{13} + p_{w} M_{14}$$

$$p_{y}' = p_{x} M_{21} + p_{y} M_{22} + p_{z} M_{23} + p_{w} M_{24}$$

$$p_{z}' = p_{x} M_{31} + p_{y} M_{32} + p_{z} M_{33} + p_{w} M_{34}$$

$$p_{w}' = p_{x} M_{41} + p_{y} M_{42} + p_{z} M_{43} + p_{w} M_{44}$$

Since p_w is always 1, the 4th column of the matrix acts as a translation

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Scaling

To scale a vector, multiply each component by a scale factor

$$M = \begin{vmatrix} S_x & 0 & 0 & 0 \\ 0 & S_y & 0 & 0 \\ 0 & 0 & S_z & 0 \\ 0 & 0 & 0 & 1 \end{vmatrix}$$

Coordinate Spaces

Coordinates are always relative to some "space"

- Object space: Local coordinate system of the object
- World space: Global coordinate system relative to the 3D "world"
- Eye / camera space: Coordinate system relative to the viewer
- When we translate objects relative to other objects, we may talk about other spaces
 - If the hand of a 3D model is rotated relative to the arm of the model, we may talk about "hand-space" or "arm-space"

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Orthonormal Basis

It's a mouthful...what does it mean?

- A vector space where all of the components are orthogonal to each other, and each is normal
 - Normal meaning unit length
 - Orthogonal meaning at right angles
 - The other meaning of normal
- Every pure rotation matrix (i.e., no scaling) is orthonormal basis
 - As is the identity matrix

Q: Given a world position for a camera, a world position to point the camera at, and an "up" direction, how can we construct a transformation using just rotations and translations?



- Q: Given a world position for a camera, a world position to point the camera at, and an "up" direction, how can we construct a transformation using just rotations and translations?
- A: We can't. We can construct an orthonormal basis from those 3 vectors



Given:

- E: Position of the eye (or camera) in world-space
- V: The point being viewed
- U: the "up" direction
- Calculate the unit vector from the viewpoint to the eye:

$$F = E - V$$
$$f = \frac{F}{|F|}$$

This is the Z axis

Calculate a vector orthogonal to the Z-axis and the up vector:

 $s = f \times u$

- This is the X-axis



Calculate a vector orthogonal to the Z-axis and the up vector:

$$s = f \times u$$

- This is the X-axis
- Calculate a vector orthogonal to the X-axis and the Z-axis:

$$t = f \times s$$

- This is the Y-axis
- Why can't we just use U?

Drop these vectors into a matrix:

$$M_{v} = \begin{bmatrix} s_{0} & s_{1} & s_{2} & -E_{0} \\ t_{0} & t_{1} & t_{2} & -E_{1} \\ f_{0} & f_{1} & f_{2} & -E_{2} \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

- The translation moves the eye to the origin



References

General information about rotation matrices and orthonormal bases:

http://en.wikipedia.org/wiki/Rotation_matrix

http://www.wikipedia.org/Orthonormal_basis

Really good explanation of arbitrary rotation matrices:

http://www.euclideanspace.com/maths/geometry/rotations/conversions/angleToMatrix/index.htm



Projection

Once objects are transformed to camera-space, they're still 3D

- The screen is still 2D
- Camera parameters (e.g., field of view) need to be applied
- Two steps remain:
 - Projection from camera space to screen space
 - Perspective divide

Projection

Perspective:

- Simulates visual foreshortening caused by the way light projects onto the back of the eye
- Represents the view volume with a frustum (a pyramid with the top cut off)
- The real work is done by dividing X and Y by Z

Orthographic:

- Represents the view volume with a cube
- Also called *parallel projection* because lines that are parallel before the projection remain parallel after

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Perspective Projection

A few parameters control the view volume:

- Near: Distance from the camera to the near viewing plane. Objects in front of this plane will be clipped
- Far: Distance from the camera to the far viewing plane. Objects behind this plane will be clipped
- θ: Field-of-view in the Y direction
- Aspect ratio: Ratio of the width of the view to the height of the view



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Perspective Projection

$$f = \cot\left(\frac{\theta}{2}\right)$$
$$M_{p} = \begin{bmatrix} \frac{f}{aspect} & 0 & 0 & 0\\ 0 & f & 0 & 0\\ 0 & 0 & \frac{far + near}{near - far} & \frac{2 \times far \times near}{near - far}\\ 0 & 0 & -1 & 0 \end{bmatrix}$$

Putting it all together

- Typically have a modeling transform, a viewing transform, and a projection
 - Combine these into a single "modelviewprojection" matrix: $M_{mvp} = M_p \times M_v \times M_m$
 - Transform a vertex by this single matrix:

```
uniform mat4 mvp;
void main(void)
```

```
gl_Position = mvp * gl_Vertex;
```

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References

http://en.wikipedia.org/wiki/3D_projection (esp. Third step: perspective transform).

http://en.wikipedia.org/wiki/Orthographic_projection_%28geometry%2 http://en.wikipedia.org/wiki/Isometric_projection


Next week...

Quiz #1

- Will cover material from last week and this week
- Hidden surface removal / occlusion
 - Backface culling
 - Painters algorithm
 - Z-buffer
 - Frustum culling
- Assignment #1, part 2
 - Assignment #1, part 1 is due

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